

15.7 Videos Guide

15.7a

- Rectangular-cylindrical conversions
 - $x = r \cos \theta$
 - $y = r \sin \theta$
 - $z = z$
 - $x^2 + y^2 = r^2$
 - $\tan \theta = \frac{y}{x}$
- The triple integral in cylindrical coordinates
 - $\iiint_E f(x, y, z) dV = \int_{\alpha}^{\beta} \int_{h_1(\theta)}^{h_2(\theta)} \int_{u_1(r \cos \theta, r \sin \theta)}^{u_2(r \cos \theta, r \sin \theta)} f(r \cos \theta, r \sin \theta) r dz dr d\theta$
 - Note that $dV = r dz dr d\theta$

Exercises:

- Sketch the solid described by the given inequalities.
 $0 \leq \theta \leq \pi/2, r \leq z \leq 2$
- Use cylindrical coordinates to evaluate $\iiint_E z dV$, where E is enclosed by the paraboloid $z = x^2 + y^2$ and the plane $z = 4$.

15.7b

- Use cylindrical coordinates to evaluate $\iiint_E (x - y) dV$, where E is the solid that lies between the cylinders $x^2 + y^2 = 1$ and $x^2 + y^2 = 16$, above the xy -plane, and below the plane $z = y + 4$.

15.7c

- Use cylindrical coordinates to find the volume of the solid that lies within both the cylinder $x^2 + y^2 = 1$ and the sphere $x^2 + y^2 + z^2 = 4$.
- Evaluate the integral by changing to cylindrical coordinates.

$$\int_{-3}^3 \int_0^{\sqrt{9-x^2}} \int_0^{9-x^2-y^2} \sqrt{x^2 + y^2} dz dy dx$$

15.7d

- Use cylindrical coordinates to find the volume of the solid that lies between the paraboloid $z = x^2 + y^2$ and the sphere $x^2 + y^2 + z^2 = 2$.